# Pencil and Paper Procedures September 2021 



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# St John the Baptist C of E Primary School Pencil and paper procedures 

## Background to the policy

This policy contains the key pencil and paper procedures that will be taught within our school. It has been written to ensure consistency and progression throughout the school and reflects a whole school agreement.
Although the focus of the policy is on pencil and paper procedures it is important to recognise that the ability to calculate mentally lies at the heart of the Mathematics Curriculum. The mental methods in will be taught systematically from Reception onwards and pupils will be given regular opportunities to develop the necessary skills. However mental calculation is not at the exclusion of written recording and should be seen as complementary to and not as separate from it. In every written method there is an element of mental processing. Sharing written methods with the teacher encourages children to think about the mental strategies that underpin them and to develop new ideas. Therefore written recording both helps children to clarify their thinking and supports and extends the development of more fluent and sophisticated mental strategies.
During their time at this school children will be encouraged to see mathematics as both a written and spoken language. Teachers will support and guide children through the following important stages:

- developing the use of pictures and a mixture of words and symbols to represent numerical activities;
- using standard symbols and conventions:
- use of jottings to aid a mental strategy;
- use of pencil and paper procedures:
- use of a calculator:
- use of specific maths manipulatives such as Numicon and Demines;
- use of ICT e.g. apps and games.

This policy concentrates on the introduction of standard symbols, the use of the empty number line as a jotting to aid mental calculation and on the introduction of pencil and paper procedures. It is important that children do not abandon jottings and mental methods once pencil and paper procedures are introduced. Therefore children will always be encouraged to look at a calculation/problem and then decide which is the best method to choose - pictures, mental calculation with or without jottings, structured recording or a calculator. Our long-term aim is for children to be able to select an efficient method of their choice (whether this be mental, written or in upper Key Stage 2 using a calculator) that is appropriate for a given task. They will do this by always asking themselves:

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'Can I do this in my head?'
'Can I do this in my head using drawings or jottings?'
'Do I need to use a pencil and paper procedure?'
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'Do I need a calculator?'
Our curriculum progression map is based on the White Rose scheme which heavily utilises the idea of 'varied fluency'. Varied fluency is an approach to teaching key concepts through a variety of concrete, abstract and pictorial methods whilst incorporating rich mathematical language.

## Aims and objectives

We will endeavour to instill the Christian Values of resilience in the teaching of the calculation methods outlined in this policy.

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| FOUNDATION STAGE |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Subtraction | Multiplication | Division |
| Use of pictures/marks to support learning: <br> Use of number lines: <br> (Counting on) <br> e.g. $7+4=11$ <br> Recording by - drawing jumps on prepared lines | Use of pictures/marks to support learning: <br> 4-1 = 3 <br> Record the number sentence alongside diagram <br> Use of number lines (numbered): $11-7$ <br> (Counting back) <br> The difference between 7 and 11 (Counting up) | Use vocabulary 'groups' 'lots of' <br> Use of pictures/marks to support learning: <br> 2 groups of 3 <br> (Showing number sentence $4 \times 2$ ) | Use of vocabulary 'sharing' <br> Use of pictures/marks to support learning: <br> 4 shared between 2 <br> (Showing number sentence $4 \div 2$ ) |

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| YEAR 1 |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Subtraction | Multiplication | Division |
| Use of pictures/marks to support learning as in Foundation Stage. Egg Method (higher ability need partitioning in place): <br> Number lines (numbered): $7+4=11$ <br> Recording by - drawing jumps on prepared lines <br> $+=$ signs and missing numbers: $\begin{array}{ll} 3+4=\square & \square=3+4 \\ 3+\square=7 & 7=\square+4 \\ \square+4=7 & 7=3+\square \\ \square+\nabla=7 & 7=\square+\nabla \end{array}$ <br> Promoting covering up of operations and numbers. | Pictures / marks: <br> Webster spent 4p. What was his change from 10p? <br> $-=$ signs and missing numbers: $\begin{array}{ll} 7-3=\square & \square=7-3 \\ 7-\square=4 & 4=\square-3 \\ \square-3=4 & 4=7-\square \\ \square-\nabla=4 & 4=\square-\nabla \end{array}$ <br> Number lines (numbered): $11-7$ <br> (Counting back) <br> The difference between 7 and 11 (Counting up) <br> Recording by - drawing jumps on prepared lines | Pictures and symbols <br> There are 3 sweets in one bag. How many sweets are there in 5 bags? <br> Children to count them all <br> Drawing groups on a line: <br> Jumping up in 'groups of' <br> $0000000-00000-$ <br> Using bead strings to support. <br> Move onto numbered number line jumping up in 'groups': | Use of vocabulary 'sharing' <br> Use of pictures/marks to support learning: <br> 12 children are shared into teams of 4 to play a game. How many teams are there? |

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| YEAR 4 |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Subtraction | Multiplication | Division |
| Partitioning expanded column method: $\begin{aligned} 42+36= & \\ 40+30 & =70 \\ 2+6 & =8 \\ & +\frac{78}{} \text { with carrying } \end{aligned}$ <br> 4 digit + 4 digit column method (with carrying) $\begin{array}{r} 3625 \\ +\frac{2517}{} \\ \hline \frac{6142}{11} \end{array}$ | Number line HTU - TU <br> Finding the difference between 184 and 56 (Counting on) <br> Partitioning standard method (HTU): <br> 457-236 $\begin{array}{r} 400+50+7 \\ -\quad 200+30+6 \\ \hline 200+20+1=221 \end{array}$ <br> Move onto a standard column method once place value is secure (cross the tens): $\begin{aligned} & 34-28= \\ & 2 \\ & 3 \\ & 3 \\ & -2 \\ & -8 \\ & 0 \end{aligned}$ | Grid method TU $\times$ TU: <br> $48 \times 56=$ If needed $2000+240+400+48=2688$ <br> Application of times tables knowledge up to $12 \times 12$ <br> 2 digit $\times 1$ digit written method $\begin{array}{r} 24 \\ \times \quad 3 \\ \hline 72 \\ \hline 1 \end{array}$ <br> 2 digit $\times 2$ digit <br> 3 digit $\times 1$ digit $326$ $\times 4$ $\frac{1304}{112}$ | Key facts box used to <br> support... <br> Horizontal number line: <br> Used where the number line is getting bigger (when using large numbers). <br> Chunking number line: |

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| YEAR 5 |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Subtraction | Multiplication | Division |
| Partitioning expanded column method: $\begin{aligned} 42+36 & = \\ 40+30= & 70 \\ 2+6= & +8 \\ & 78 \end{aligned}$ <br> Formal method. <br> Showing numbers carried underneath $\begin{array}{r} 358 \\ +\quad 73 \\ \hline 431 \\ \hline 11 \end{array}$ <br> Extend to numbers with at least four digits $\begin{aligned} & 3587+675=4262 \\ &+\quad 675 \\ & \hline 4262 \end{aligned} \quad .$ <br> Revert to expanded methods if the children experience any difficulty. Extend to decimals. | Finding differences by counting on. <br> Partitioning standard method supported by number line: $4008-2995=1013$ <br> Moving onto numbers with two decimal places. E.g. $£ 235+£ 33.75$. <br> Move onto a standard column method once place value is secure (Th H T U): 2184-156 <br> Bigger than 4 digit-4 digit $\begin{array}{r} 21^{7} 8^{1} 4 \\ -1156 \\ \hline 1028 \\ \hline \end{array}$ | Grid method HTU $\times$ TU: <br> $372 \times 24$ is approximately $400 \times 20=$ <br> 8000 <br> Extend to decimals with up to two decimal places. <br> Application of times tables knowledge up to $12 \times 12$ ```Written method 4 digit \(\times 1\) digit 2341 \(\times \quad 6\) 14046 3 digit \(\times 2\) digit 278 \(\times \quad 36\) 1722 \(+8610\) 10332``` | Key facts box used to <br> support... $\begin{array}{\|l\|} \hline 5 x \\ 10 x \\ 100 x \\ \hline \end{array}$ <br> Vertical chunking number line: (if necessary make the steps smaller) $61 \div 8=$ <br> Chunking method: <br> $72 \div 5$ lies between $50 \div 5=10$ and $100 \div 5=20$ $\begin{aligned} & 72 \\ &- \frac{50}{22} \\ &-\quad(10 \text { groups }) \text { or }(10 \times 5) \\ &- \frac{20}{2} \\ &(4 \text { groups }) \text { or }(4 \times 5) \end{aligned}$ <br> Answer: 14 remainder 2 <br> Bus shelter secured: $3 \begin{array}{\|c} 325 \\ \end{array}$ |

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| YEAR 6 |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition | Subtraction | Multiplication | Division |
| Partitioning: <br> Partition into hundreds, tens, ones and decimal fractions and recombine <br> Either partition both numbers and recombine or partition the second number only e.g. $\begin{aligned} 35.8+7.3 & =35.8+7+0.3 \\ & =42.8+0.3 \\ & =43.1 \end{aligned}$ <br> Standard Column Method: <br> Extend to numbers with any number of digits and decimals with 1 and 2 decimal places. $\begin{aligned} & 124.9+117.25=242.15 \\ & 124.90 \\ & +\frac{117.25}{\frac{242.15}{11}} \end{aligned}$ <br> Revert to expanded methods if the children experience any difficulty. <br> Extend to decimals (either one or two decimal places). | Standard compact method: $\begin{array}{r} 39 \\ 410108 \\ -\quad 2995 \\ \hline 1013 \\ \hline \end{array}$ <br> Moving onto decimal numbers | Standard Method: $\begin{aligned} & 236 \times 23= \\ & 236 \\ & \begin{array}{r} 27 \\ 1652 \\ +4720 \\ 6372 \end{array} \end{aligned}$ <br> Time Tables All up to $12 \times 12$ | Bus shelter secured: $\begin{aligned} & 325 r^{3} \quad{ }^{9717} \end{aligned}$ |

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## POLICY REASONING

- The above policy shows the main methods to be employed by class teachers for on track children in each particular year.
- There is scope for class teachers to 'layer' up or back in their method choice depending on children's ability.
- For those children who cannot access the main written method depicted for their year, class teachers should make use of the wide range of alternative written methods available so every child has a successful age appropriate written method to choose from. The policy therefore allows teachers to individualise where necessary.
- Year 4,5,6 integers are much larger than those used in Year 3. As a result, although counting back will be done orally, written methods where counting back is used can be unwieldy and inappropriate. Therefore written methods in subtraction and division change from counting back to counting up. It is assumed that the children will understand the concept of the operation as a result of earlier counting back methods employed in Years 3, 2 and 1.

Reviewed: September 2021
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Reviewed by: P Seaton
Governor:

