

Pencil and Paper Procedures September 2021



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St John the Baptist C of E Primary School

Pencil and paper procedures

Background to the policy

This policy contains the key pencil and paper procedures that will be taught within our school. It has been written to ensure consistency and progression throughout the school and reflects a whole school agreement.

Although the focus of the policy is on pencil and paper procedures it is important to recognise that the ability to calculate mentally lies at the heart of the Mathematics Curriculum. The mental methods in will be taught systematically from Reception onwards and pupils will be given regular opportunities to develop the necessary skills. However mental calculation is not at the exclusion of written recording and should be seen as complementary to and not as separate from it. In every written method there is an element of mental processing. Sharing written methods with the teacher encourages children to think about the mental strategies that underpin them and to develop new ideas. Therefore written recording both helps children to clarify their thinking and supports and extends the development of more fluent and sophisticated mental strategies.

During their time at this school children will be encouraged to see mathematics as both a written and spoken language. Teachers will support and guide children through the following important stages:

- developing the use of pictures and a mixture of words and symbols to represent numerical activities;
- using standard symbols and conventions;
- use of jottings to aid a mental strategy;
- use of pencil and paper procedures;
- use of a calculator;
- use of specific maths manipulatives such as Numicon and Demines;
- use of ICT e.g. apps and games.

This policy concentrates on the introduction of standard symbols, the use of the empty number line as a jotting to aid mental calculation and on the introduction of pencil and paper procedures. It is important that children do not abandon jottings and mental methods once pencil and paper procedures are introduced. Therefore children will always be encouraged to look at a calculation/problem and then decide which is the best method to choose - pictures, mental calculation with or without jottings, structured recording or a calculator. Our long-term aim is for children to be able to select an efficient method of their choice (whether this be mental, written or in upper Key Stage 2 using a calculator) that is appropriate for a given task. They will do this by always asking themselves:

'Can I do this in my head?'

'Can I do this in my head using drawings or jottings?'

'Do I need to use a pencil and paper procedure?'





'Do I need a calculator?'

Our curriculum progression map is based on the White Rose scheme which heavily utilises the idea of 'varied fluency'. Varied fluency is an approach to teaching key concepts through a variety of concrete, abstract and pictorial methods whilst incorporating rich mathematical language.

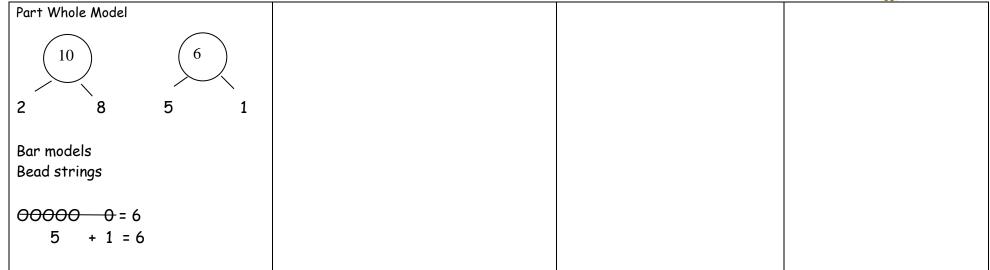
Aims and objectives

We will endeavour to instill the Christian Values of resilience in the teaching of the calculation methods outlined in this policy.



FOUNDATION STAGE				
Addition	Subtraction	Multiplication	Division	
Use of pictures/marks to support	Use of pictures/marks to support learning:	Use vocabulary	Use of vocabulary 'sharing'	
<u>learning:</u>		'groups'		
	4 - 1 = 3	'lots of'	<u>Use of pictures/marks to</u> <u>support learning:</u>	
		<u>Use of pictures/marks to support</u>		
	@	<u>learning:</u>	4 shared between 2	
		2	(Showing number sentence 4 ÷ 2)	
		2 groups of 3		
		(Showing number sentence 4 x 2)		
+ =	Record the number sentence alongside diagram			
	<u>Use of number lines (numbered):</u>			
2 + = 3	11 - 7			
	(Counting back)			
(📍)				
	0 1 2 3 4 5 6 7 8 9 10 11 12			
2 + 1 = 3				
Use of number lines:				
(Counting on) e.g. 7 + 4 = 11	The difference between 7 and 11 (Counting up)			
Recording by - drawing jumps on prepared lines	0 1 2 3 4 3 0 7 6 9 10 11 12			







	YEAR 1		
Addition	Subtraction	Multiplication	Division
Use of pictures/marks to support	<u>Pictures / marks:</u>	Pictures and symbols	Use of vocabulary 'sharing'
learning as in Foundation Stage.	Webster spent 4p. What was his change	There are 3 sweets in one bag.	
Egg Method (higher ability need	from 10p?	How many sweets are there in 5	<u>Use of pictures/marks to</u>
<u>partitioning in place):</u>	\$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$ \$\$	bags?	<u>support learning:</u>
10 10 20			12 children are shared into teams
		Children to count them all	of 4 to play a game. How many teams are there?
$\left(\begin{array}{c}16\end{array}\right) + \left(12\right) = \left(28\right)$	- = signs and missing numbers:		
	7 - 3 = 🗆 🗆 = 7 - 3	Drawing groups on a line:	$12 \div 3 = 4$
6 2 8	7 - 🗆 = 4 4 = 🗆 - 3	Jumping up in 'groups of'	
Number lines (numbered):	□ - 3 = 4		
	$\Box - \nabla = 4 \qquad \qquad 4 = \Box - \nabla$		
7 + 4 = 11		Using bead strings to support.	
	Number lines (numbered):		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	11 - 7	AA	
	(Counting back)	Move onto numbered number line	
Recording by - drawing jumps on prepared lines		jumping up in 'groups':	
<u>+ = signs and missing numbers:</u>			
- signs and missing humbers.			
3 + 4 = 🗆 🗆 = 3 + 4			
3 + □ = 7 7 = □ + 4	The difference between 7 and 11		
□ + 4 = 7 7 = 3 + □	(Counting up)		
$\Box + \nabla = 7 \qquad \qquad 7 = \Box + \nabla$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
Promoting covering up of operations and			
numbers.	Recording by - drawing jumps on prepared		
	lines		



		100110
Add column method with partition		
e.g 18 Part who $+\frac{14}{32}$ 24 1 20 4		



YEAR 2			
Addition	Subtraction	Multiplication	Division
+ = signs and missing numbers:Continue using a range of equations as inYear 1 but with appropriate, larger numbers.Extend to $14 + 5 = 10 + \Box$ and adding three numbers $32 + \Box + \Box = 100$ $35 = 1 + \Box + 5$	- = signs and missing numbers: Continue using a range of equations as in Year 1 but with appropriate numbers. Extend to 14 + 5 = 20 - □ <u>Number lines:</u> (Counting back) 37 - 12 = 25	Arrays and repeated addition: Read as rows - 2 lots of 4 • • • • • 4 × 2 • • • • •	Understand division as sharing and grouping <u>Use of pictures/marks to support</u> <u>learning:</u> 6 ÷ 2
Egg Method (need partitioning in place):17 + 12 = 2910101020 (17) + (12) = (29)	25 27 37 -2 -10	<u>repeated addition:</u> <u>4 x 2</u> is 2 + 2 + 2 + 2	Sharing - 6 sweets are shared between 2 people. How many do they have each?
7 2 9 Move onto units crossing the tens boundary: 25 + 36 = 61 20 30 60 25 + 36 = 61 5 6 11 Number lines using partitioning knowledge: 23 + 12 = 35	Finding the difference between 39 and 42 (Counting up) 42 - 39 = 3 +1 $+239$ 40 42	0 1 2 3 4 5 6 7 8	Use of number line for grouping: 6 ÷ 2 Grouping - There are 6 sweets. How many people can have 2 each? (How many groups of 2 make 6?) 3 2 1 groups groups group
+10 23 33 Recording by - drawing jumps on prepared lines (higher ability draw own)			0 2 4 6 "How many groups of 2 can you make from 6?"



Addition	<u>Subtraction</u>
2 digit + 1 digit column method	2 digit - 1 digit column method
e.g. 12	e.g. 48
+ <u>4</u>	- <u>5</u>
<u>16</u>	<u>43</u>
2 digit + 2 digit 2 digit + 2 digit (crossing 10s) e.g. 42 move on to 47 + <u>33</u> + <u>18</u> <u>75</u> <u>65</u> 1	2 digit - 2 digit 2 digit - 2 digit (with borrowing and exchanging) 76 move on to 2 3 ¹ 4 - <u>32</u> <u>44</u> <u>17</u>



	YEAR 3		
Addition	Subtraction	Multiplication	Division
<u>Number line:</u> 23 + 12 = 35	<u>Number line method TU - TU:</u> Finding the difference between 84 and 56 (Counting on)	<u>Written</u> Method 2 digit × 1 digit mental 23	<u>Informal diagram:</u> 30 ÷ 5 = 6
+10 23 23 Recording by - drawing jumps on prepared lines (higher ability draw own)	84 - 56 = 28 +4 +20 +4	X <u>8</u> <u>184</u> 12 <u>Grid Method TU x U:</u>	30 - 5 = 25 25 - 5 = 20 20 - 5 = 15 15 - 5 = 10 10 - 5 = 5
Egg Method (need partitioning in place): crossing the tens boundary: $25 + 36 = 61$ $20 \qquad 30 \qquad 60$ $(25) + (36) = (61)$	56 60 80 84 Subtracting by adjusting from a multiple of 10 i.e9 = -10 + 1 / -11 = -10 -1 <u>Partitioning standard method (TU):</u> 57 - 36 50 + 7	$23 \times 8 =$ $23 \times 8 =$ $1 \qquad 2 \qquad 3 \qquad \times$ $1 \qquad 2 \qquad 8$ $1 \qquad 8 \qquad 4$	5 - 5 = 0 6 groups of 5 <u>Number line method:</u> Used where the number line is getting smaller. 30 ÷ 5 = 6
$5 \ 6 \ 11$ $\frac{Move \text{ onto partitioning:}}{42 + 36 =}$ $40 + 30 = \ 70$ $2 + 6 = \ + \ 8$ $- \ 78$	50 + 7 $- 30 + 6$ $20 + 1 = 21$ Move onto a standard column method once place value is secure (not crossing the ten's boundary): 36 - 24 = 12 $3 6$ $- 2 4$ $-1 2$	Long multiplication standard method TU by U only: 23 x 8 = 184 long 2 3 X 8 $3 \times 8 = 24$ $20 \times 8 = 160 + 184$	1 2 3 4 5 6 30 25 20 15 10 5 0



Addition	Subtraction	
2 digit + 2 digit (with carrying)	2 digit - 2 digit (to include borrowing)	Short 23
		X <u>8</u>
47	² 3 ¹ 4	<u>184</u>
+ <u>18</u> <u>65</u>	- <u>17</u>	<u>12</u>
<u>65</u>	<u>17</u>	Application of times tables
1	and 3 digit - 3 digit	knowledge (2,5,10) and 3,4, 8
	<i>5</i> ⁵ 6 ¹ 3	times table
Use the same method for adding:	- <u>3 2 7</u>	
3 digit + 1 digit 236	236	
3 digit + 2 digit + <u>327</u>		
3 digit + 3 digit <u>563</u>		
1		



	YEAR 4		
Addition	Subtraction	Multiplication	Division
	Number line HTU - TU	Grid method TU x TU:	Key facts box used to
Partitioning expanded column method: 42 + 36 =	Finding the difference between 184 and 56 (Counting on)	48 x 56 = If needed	<u>support</u> 5 x 10 x
40 + 30 = 70		X 50 6	20 x
2 + 6 = + 8	184 - 56 = 128	40 2000 240	100 x
78 with carrying	.4 .40 .80 .4	8 400 48	
4 digit + 4 digit column method (with carrying) 3625 + <u>2517</u> <u>6142</u> 1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2000 + 240 + 400 + 48 = 2688 Application of times tables knowledge up to 12 x 12 $2 \text{ digit } x 1 \text{ digit written method}$ 24 $X \underline{3}$ $\frac{72}{12}$ 1 $2 \text{ digit } x 2 \text{ digit}$ 57 $X \underline{62}$ 114 $\underline{3420}$ $\underline{3534}$ $3 \text{ digit } x 1 \text{ digit}$ 326 $X \underline{4}$ $\underline{1304}$ 112	Horizontal number line: Used where the number line is getting bigger (when using large numbers). $37 \div 5 = 7 r2$ 1 2 3 4 5 6 7 (groups) 12 3 4 5 6 7 (groups) 12 3 4 5 6 7 (groups) 15 20 25 30 35 37 Chunking number line: $37 \div 5 = 7 r2$ 6 groups 1 group -30 - 6 72 - 30 7 - 2



		- 10011-
Subtraction 4 digit - 4 digit (with borrowing) ⁵ 6 ¹ t ³ A ¹ 2 - <u>3 6 2 5</u> <u>2 5 1 7</u>	Long multiplication standard method TU by TU by partitioning: $23 \times 86 =$ $23 \times 86 =$ $6 \times 3 = 18$ $6 \times 20 = 120$ $80 \times 3 = 240$ $80 \times 20 = 1600 +$ 1978	



	YEAR 5		
Addition	Subtraction	Multiplication	Division
Addition Partitioning expanded column method: 42 + 36 = 40 + 30 = 70 2 + 6 = + 8 -78 Formal method. Showing numbers carried underneath 358 + 73 -431 11 Extend to numbers with at least four digits 3587 + 675 = 4262 3587 $+ \frac{675}{4262}$ 111 Revert to expanded methods if the children experience any difficulty. Extend to decimals.		MultiplicationGrid method HTU x TU: 372×24 is approximately $400 \times 20 = 8000$ x 300 70 2 20 6000 4 1200 280 8 Extend to decimals with up to two decimal places.Application of times tables knowledge up to 12×12 Written method 4 digit $\times 1$ digit 2341 X 6 14046 3 digit $\times 2$ digit 27.8 X 3.6 $1.7.2$ $+8.6.10$ $10.3.3.2$	Division <u>Key facts box used to</u> <u>support</u> $5 \times 10 \times 100 \times 1000 \times 100 \times 100 \times 100 \times 1000 \times 100 \times 1000 \times 100 \times 100 \times 100$



YEAR 6				
Addition	Subtraction	Multiplication	Division	
Partitioning:	<u>Standard compact method:</u>	<u>Standard Method:</u> 236 x 23 =	Bus shelter secured:	
Partition into hundreds, tens, ones and decimal fractions and recombine Either partition both numbers and recombine or partition the second number only e.g. 35.8 + 7.3 = 35.8 + 7 + 0.3 = 42.8 + 0.3 = 43.1 +7 $+0.335.8$ 42.8 $43.1Standard Column Method:Extend to numbers with any number ofdigits and decimals with 1 and 2 decimalplaces.124.9 + 117.25 = 242.15124.90+ 117.25 = 242.15124.90+ 117.25 = 242.15Revert to expanded methods if the childrenexperience any difficulty.Extend to decimals (either one or twodecimal places).$	3 9 4 10 10 8 - <u>2 9 9 5</u> 1 0 1 3 Moving onto decimal numbers	236 x 23 = 2 3 6 $x \frac{27}{1652}$ $+ \frac{4720}{6372}$ Time Tables All up to 12 x 12	325 r2 3 9717	



POLICY REASONING

- The above policy shows the main methods to be employed by class teachers for on track children in each particular year.
- There is scope for class teachers to 'layer' up or back in their method choice depending on children's ability.
- For those children who cannot access the main written method depicted for their year, class teachers should make use of the wide range of alternative written methods available so every child has a successful age appropriate written method to choose from. The policy therefore allows teachers to individualise where necessary.
- Year 4, 5, 6 integers are much larger than those used in Year 3. As a result, although counting back will be done orally, written methods where counting back is used can be unwieldy and inappropriate. Therefore written methods in subtraction and division change from counting back to counting up. It is assumed that the children will understand the concept of the operation as a result of earlier counting back methods employed in Years 3, 2 and 1.

Reviewed: September 2021 Review: September 2023

Reviewed by: P Seaton Governor: